

Last/Family Name:

First/Given Name:

Student ID:



## MATH 37181 FINAL PART A SPRING 2021

- INSTRUCTIONS.
- If you don't have a printer or tablet:
    - write your declaration "I declare that: this is my own work ..." at the start of your blank page for Part A;
    - write your answers in the same order and format as this file on blank paper.
  - Write your name and student ID on the top of your first page.
  - Upload your scan to Canvas - Assignments - Final Exam Part A as a **single PDF file**.
  - Name your file using your last-name, student ID number and -PartA, eg: Elder12345678-PartA.pdf
  - Show all steps and working out. Clearly identify your answers for the multiple choice. (Eg write A1:F, A2:F, A3:F, A4:F, A5:F on your first page, or circle on a printed page.)
  - You may use a basic scientific calculator for calculations. For Question A3 only you may also use the symbolab website.

Part A has **5 multiple choice** and **2 long answer questions** worth a total of 15 marks. You should spend roughly 1 hour on this part.

I declare that: this is my own work, I have not used Discord/Wechat/Facebook etc or asked anyone anything during the exam, I have not posted screenshots or uploaded anything to an online site, I have not used any phone apps except a basic calculator app and Camscanner or other scanning app to scan my work, and I have not looked at any websites other than Canvas to download/upload, and symbolab for Question A3.

(sign your name here) \_\_\_\_\_

A1. (1 mark) The statement

$$\neg(p \vee \neg(q \wedge \neg r))$$

is logically equivalent to

**A.**  $p \wedge (\neg q \wedge \neg r)$

**D.**  $\neg(p \vee \neg q) \vee \neg r$

**B.**  $\neg p \wedge (q \vee \neg r)$

**E.**  $\neg(p \vee r) \wedge q$

**C.**  $\neg p \vee (\neg q \wedge \neg r)$

**F.** none of (A)–(E).

A2. (1 mark) Consider the function  $f : \mathbb{N} \rightarrow \mathbb{Z}$  defined by the *recursive* definition <sup>1</sup>

$$\begin{aligned} f(0) &= 2 \\ f(1) &= -1 \\ f(n) &= n * f(n-2) \quad n > 1. \end{aligned}$$

The value of  $f(7)$  is

**A.** 96

**D.** -177

**B.** 768

**E.** -420

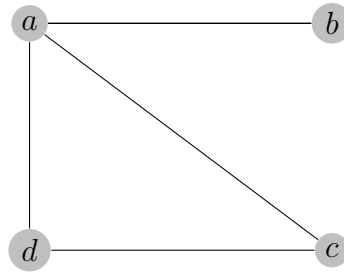
**C.** -105

**F.** none of (A)–(E).

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<sup>1</sup>\* means multiplied. Eg  $4 * 5 = 20$

A3. (1 mark) Let  $G$  be an undirected graph displayed here:



(a) Draw an adjacency matrix for this graph.

(b) The number of paths of length 8 from the vertex labeled  $a$  to the vertex labelled  $b$  is <sup>2</sup>

A. 45

D. 197

B. 76

E. 137

C. 152

F. none of (A)–(E).

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<sup>2</sup>You may use <https://www.symbolab.com/> for this question.

A4. (1 mark) Consider the following fragment of pseudocode:

```

procedure (n int)
temp := 0
for i := 1 to n-1 do
    for j := 1 to i do
        temp := temp + i*j
    print temp

```

On input  $n = 10$ , how many times is the command `print temp` executed?

- |       |                     |
|-------|---------------------|
| A. 55 | D. 100              |
| B. 45 | E. 20               |
| C. 10 | F. none of (A)–(E). |

A5. (1 mark) To show that the set theory statement

$$\overline{A} \cap (B \cup C) = (B \cap \overline{A}) \cup C$$

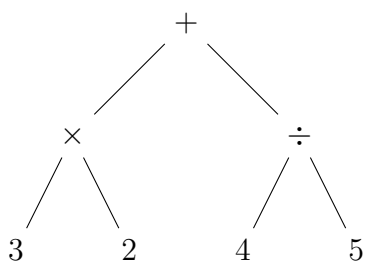
is incorrect, we could use the following example:

- A.  $\mathcal{U} = \{1, 2, 3, 4, 5\}, A = \{1, 2\}, B = \{3, 4\}, C = \{5\}$
- B.  $\mathcal{U} = \{1, 2, 3, 4\}, A = \{1, 2\}, B = \{2, 3\}, C = \{4\}$
- C.  $\mathcal{U} = \{1, 2\}, A = \emptyset, B = \{1\}, C = \{2\}$
- D.  $\mathcal{U} = \{1, 2, 3, 4\}, A = \{2, 4\}, B = \{1, 3\}, C = \{4\}$
- E.  $\mathcal{U} = \{1, 2, 3\}, A = \{1\}, B = \{2\}, C = \{3\}$
- F. none of (A)–(E).

A6. (5 marks) Prove that  $\exists c \in \mathbb{N}$  so that  $n! > 20^n$  for all  $n \geq c$ .

A7. (5 marks)

(a) Give the in-order traversal of the following:



(b) Give the tree corresponding to the arithmetic expression  $\frac{x \times y}{f + 7} - \left(c + \frac{z - v}{d}\right)$

(c) Give the post-order traversal of the tree in part (b)

END OF PART A