

## Tutorial 5

1. Consider the LP

$$\begin{array}{ll} \min & -x_1 - 2x_2 \\ \text{s.t.} & x_1 + x_2 \geq 4 \\ & 3x_1 + 2x_2 \leq 24 \\ & x_1, x_2 \geq 0. \end{array}$$

Solve this LP with two phase Simplex method (and compare the solution with that of the big- $M$  method).

2. Use the two phase Simplex method or big- $M$  method to determine whether there is a feasible solution to the following LP (Note: You do **not** need to find an optimal solution).

$$\begin{array}{ll} \min & 3x_1 - 2x_2 \\ \text{s.t.} & x_1 + 4x_2 + 4x_3 \leq 2 \\ & x_2 + x_3 = 1 \\ & x_1, x_2, x_3 \geq 0. \end{array}$$

3. Solve the following LP with the two phase Simplex method (and compare the solution with that of the big- $M$  method):

$$\begin{array}{ll} \min & 3x_1 - 2x_2 + x_3 \\ \text{s.t.} & -3x_1 + 3x_2 + 2x_3 \geq 10 \\ & 2x_1 - 2x_2 - x_3 \geq 16 \\ & x_1, x_2, x_3 \geq 0. \end{array}$$